



INTRODUCTION TO CONTROL (034040)

TUTORIAL 11

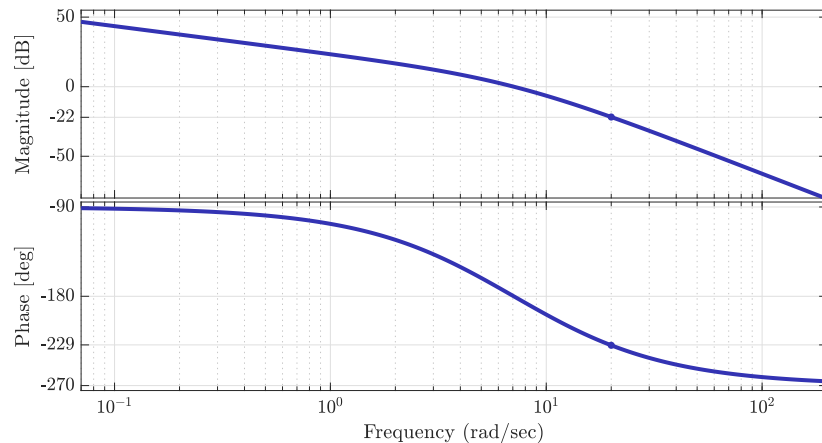


Fig. 1: Bode plot of  $P(s)$  in Question 1

**Question 1.** Fig. 1 presents the Bode plot of

$$P(s) = \frac{750}{s(s+5)(s+10)}$$

Design a stabilizing controller  $C(s)$  in the unity-feedback configuration so that

1. closed-loop bandwidth  $\omega_b \geq 20$  [rad/sec],
2. phase margin  $\mu_{ph} \geq 45^\circ$ ,
3. steady-state error for a step reference signal does not exceed 1% of the step height,
4. steady-state error for a step load disturbance does not exceed 1% of the step height.

Repeat it with the phase margin bound  $\mu_{ph} \geq 35^\circ$ , explain differences.

**Question 2** (self study). Consider a DC motor like that in Lecture 11 controlled in the unity-feedback scheme. Assume that a loop delay of 1.5 [s] is also present in the loop, i.e. the plant transfer function is now

$$P(s) = \frac{1}{s(s+2)} e^{-1.5s}$$

Consider the following closed-loop specifications:

- zero steady-state error for a step in  $r$
- zero steady-state error for a step in  $d$
- phase margin  $\mu_{ph} \geq 45^\circ$ .

Design stabilizing controllers  $C$  for these specifications under the following requirements on the crossover frequency:

1.  $\omega_c = 0.05$  [rad/sec],
2.  $\omega_c = 0.5$  [rad/sec],
3.  $\omega_c = 1$  [rad/sec].